Notice

- Due dates
 - Project Checkpoint Presentation 1 (on the 31st)
 - 15-17 min presentation + 3-5 min Q&A
 - Presentation MUST cover:
 - A research problem your team chose
 - A review of the prior work relevant to your problem
 - [Option #1] How is your work different from the prior work?
 [Option #2] Papers your team will reproduce the results (in detail)
 - Your team's next steps
- Sign-up (on Canvas)
 - Scribe Lecture Note
 - In-class Paper Presentation / Discussion



CS 499/599: Machine Learning Security 01.26: Adversarial Examples (AE)

Mon/Wed 12:00 – 1:50 pm

Sanghyun Hong

sanghyun.hong@oregonstate.edu





Recap

- ML Matters
- Evasion (Test-time Adversarial) Attack
 - Threat model
 - Attacks:
 - White-box:
 - FGSM / BIM / C&W / PGD attacks
 - Black-box:
 - Practicality
 - Transfer-based / Optimization-based attacks
 - Defenses:
 - Adversarial training
 - System-level defenses (e.g., FeatureSqueezing)
 - Certified (provable) defenses



Topics for Today

- Certified (Provable) Defenses
 - Motivation
 - Robustness [?!]
 - Make ML models robust
 - Certified robustness
 - (Randomized) Smoothing
 - Guarantee
 - Practicality
 - Implementation
 - Evaluate the robustness
 - Upper-bound / Lower-bound
 - Real-world scenarios
 - Conclusions



Certified Adversarial Robustness via Randomized Smoothing

Jeremy Cohen, Elan Rosenfeld, and J. Zico Kolter

Denoised Smoothing: A Provable Defense for Pretrained Classifiers

Hadi Salman, Mingie Sun, Greg Yang, Ashish Kapoor, and J. Zico Kolter

Topics for Today

- Robust Models
 - Motivation
 - Robustness [?!]
 - Make ML models robust
 - Certified robustness
 - (Randomized) Smoothing
 - Guarantee
 - Practicality
 - Implementation
 - Evaluate the robustness
 - Upper-bound / Lower-bound
 - Real-world scenarios
 - Conclusions



Motivation

- Questions:
 - What does it mean by "robust" in ML?
 - How can we make ML models "robust"?



Motivation

- Questions:
 - What does it mean by "robust" in ML?
 - How can we make ML models "robust"?
- Problems in the previous defenses
 - Are they "really" robust?
 - Are these solutions "scalable"?





Motivation - cont'd

- Research Questions:
 - RQ 1: What is the "upper-bound" of the robustness?
 - RQ 2: How can you "certify" that yours is the upper-bound?
 - RQ 3: How can we make the certification "computationally feasible"?



Robustness

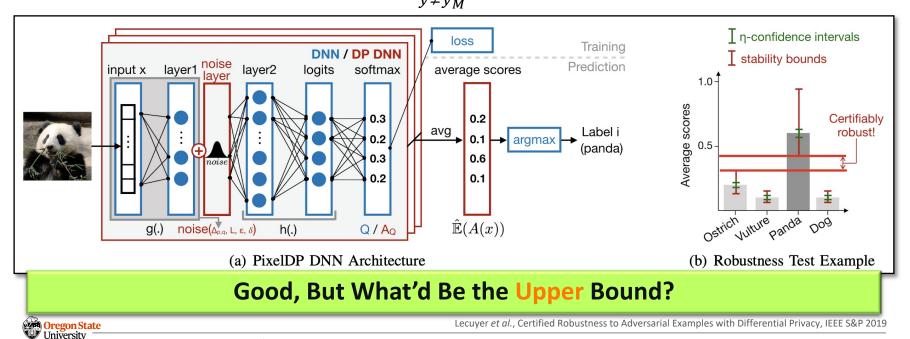
- Suppose:
 - (x, y): a test-time input and its oracle label
 - $x + \delta$: an adversarial example of x with small l_p -bounded (ε) perturbation δ
 - *f*: a neural network
- Robustness
 - For any δ where $||\delta||_p \leq \varepsilon$ and the most probable class y_M for $f(x + \delta)$
 - Make f to be $P[f(x + \delta) = y_M] > \max_{y \neq y_M} P[f(x + \delta) = y]$



Prior Work on Certified Robustness

- Robustness with certificates
 - For any δ where $||\delta||_p \leq \varepsilon$ and the most probable class y_M for $f(x + \delta)$

- Make f to be
$$P[f(x + \delta) = y_M] > \max_{y \neq y_M} P[f(x + \delta) = y] + \eta$$



Topics for Today

- Robust Models
 - Motivation
 - Robustness [?!]
 - Make ML models robust
 - (Certified; provable) Robustness
 - (Randomized) Smoothing
 - Guarantee
 - Practicality
 - Implementation
 - Evaluate robust models
 - Upper-bound / Lower-bound
 - Real-world scenarios
 - Conclusions (and Implications)



• Smoothing:

- In image processing: reduce noise (high frequency components)
- In neural networks: make f less sensitive to noise

• Randomized:

- In statistics: the practice of using chance methods (random)
- In this work: add Gaussian random noise $\sim N(0, \sigma^2 I)$ to the input x
- Randomized Smoothing:
 - [Train w. Gaussian noise to f's input]
 [to make it less sensitive to adversarial perturbations]

$$g(x) = \operatorname*{arg\,max}_{c \in \mathcal{Y}} \mathbb{P}(f(x + \varepsilon) = c)$$

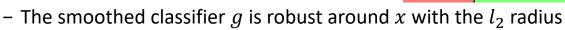
where $\varepsilon \sim \mathcal{N}(0, \sigma^2 I)$





Randomized Smoothing: Guarantee

- Suppose
 - f: a base classifier (e.g., a NN)
 - $\mathbf{P}[f(x+\delta) = c_A] \approx P_A$
 - $-\max_{y\neq y_M} \mathbb{P}[f(x+\delta)=y] \approx P_B$
- Certified robustness



$$R = \frac{\sigma}{2} (\Phi^{-1}(\underline{p_A}) - \Phi^{-1}(\overline{p_B}))$$

- Observations
 - f can be any classifier, e.g., convolutional neural networks, ...
 - R (Guarantee) is large when we use high noise, c_A is high, or c_B is low
 - R (Guarantee) is infinite as $P_A \approx 1$ and $P_B \approx 0$



 \bar{p}_{A}

 $\overline{p_B}$

Randomized Smoothing: Practicality

Conversion to a robust classifier

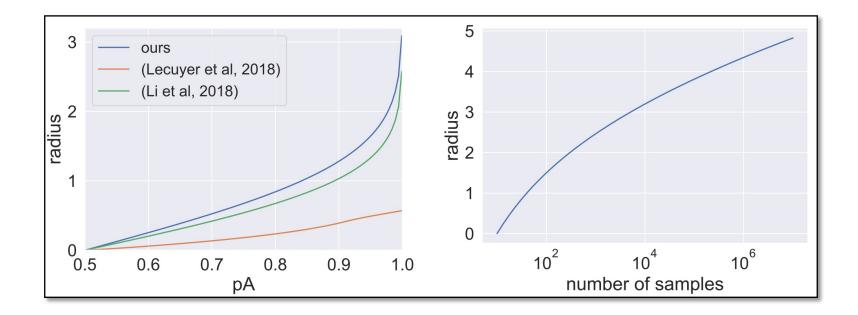
```
Pseudocode for certification and prediction# evaluate g at xfunction PREDICT(f, \sigma, x, n, \alpha)counts \leftarrow SAMPLEUNDERNOISE(f, x, n, \sigma)\hat{c}_A, \hat{c}_B \leftarrow top two indices in countsn_A, n_B \leftarrow counts[\hat{c}_A], counts[\hat{c}_B]if BINOMPVALUE(n_A, n_A + n_B, 0.5) \leq \alpha return \hat{c}_Aelse return ABSTAIN# certify the robustness of g around xfunction CERTIFY(f, \sigma, x, n_0, n, \alpha)counts0 \leftarrow SAMPLEUNDERNOISE(f, x, n_0, \sigma)
```

 $\hat{c}_A \leftarrow \text{top index in counts0}$ $\hat{c}_A \leftarrow \text{top index in counts0}$ $\text{counts} \leftarrow \text{SAMPLEUNDERNOISE}(f, x, n, \sigma)$ $\underline{p_A} \leftarrow \text{LOWERCONFBOUND}(\text{counts}[\hat{c}_A], n, 1 - \alpha)$ **if** $\underline{p_A} > \frac{1}{2}$ **return** prediction \hat{c}_A and radius $\sigma \Phi^{-1}(\underline{p_A})$ **else return** ABSTAIN Guarantee the probability of *PREDICT* returning a class other than g(x) is α

CERTIFY returns a class c_A and a radius R for the g(x) with the probability α

Randomized Smoothing: Practicality

• Conversion to a robust classifier





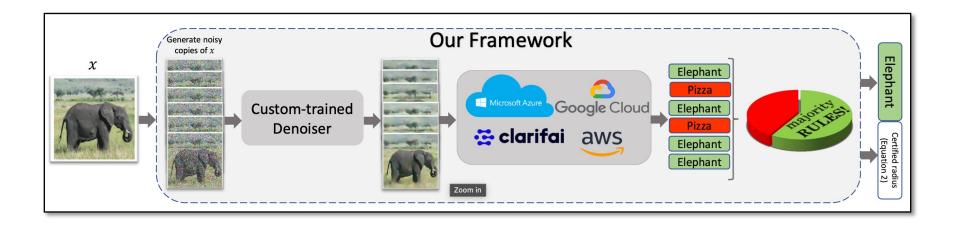
Randomized Smoothing: Implementations

- Conversion to a robust classifier
 - Train a base classifier f with noised samples $\sim N(x, \sigma^2 I)$ with x's oracle label
 - Train a denoiser $D_{\theta}: \mathbb{R}^d \to \mathbb{R}^d$ that removes the input perturbations for f
- Problem:
 - Should we re-train all the classifiers, already trained and on-service?
 - How much would it be practical? [Consider ImageNet models]
- Solution:
 - Denoised smoothing: add a denoiser on top of a pre-trained classifier



Randomized Smoothing: Implementations

- Conversion to a robust classifier
 - Train a base classifier f with noised samples $\sim N(x, \sigma^2 I)$ with x's oracle label
 - Train a denoiser $D_{\theta}: \mathbb{R}^d \to \mathbb{R}^d$ that removes the input perturbations for f





Denoised Smoothing

- Goal
 - Not to train *f* on noise
 - But, to provide certification to f
- Formally, We want
 - This: $g(x) = \underset{c \in \mathcal{Y}}{\operatorname{arg\,max}} \mathbb{P}[f(x + \delta) = c]$ where $\delta \sim \mathcal{N}(0, \sigma^2 I)$
 - To be this: $g(x) = \operatorname*{arg\,max}_{c \in \mathcal{Y}} \mathbb{P}[f(\mathcal{D}_{\theta}(x+\delta)) = c]$ where $\delta \sim \mathcal{N}(0, \sigma^2 I)$
- Train D_{θ}
 - MSE objective: Just train D_{θ} to remove Gaussian noise $L_{\text{MSE}} = \underset{S,\delta}{\mathbb{E}} \|\mathcal{D}_{\theta}(x_i + \delta) x_i\|_2^2$
 - + Stability objective: (White-box) Preserve f's predictions $L_{\text{Stab}} = \mathbb{E}_{\mathcal{S},\delta}^{\mathcal{S},\delta} \ell_{\text{CE}}(F(\mathcal{D}_{\theta}(x_i + \delta)), f(x_i))$



Topics for Today

Robust Models

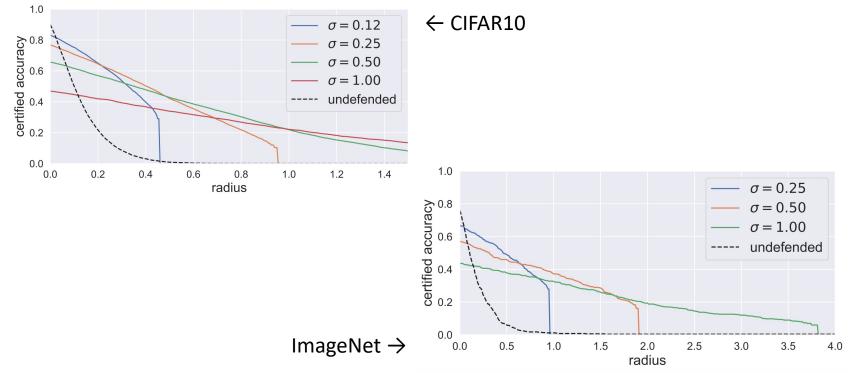
- Motivation
 - Robustness [?!]
 - Make ML models robust
 - (Certified; provable) Robustness
- (Randomized) Smoothing
 - Guarantee
 - Practicality
 - Implementation
- Evaluate robust models
 - Upper-bound / Lower-bound
 - Real-world scenarios
- Conclusions (and Implications)



- Setup
 - CIFAR10: ResNet-110 and its full test-set
 - ImageNet: ResNet-50 and 500 random chosen test-set samples
- Measure
 - (approximate) Certified test-set accuracy

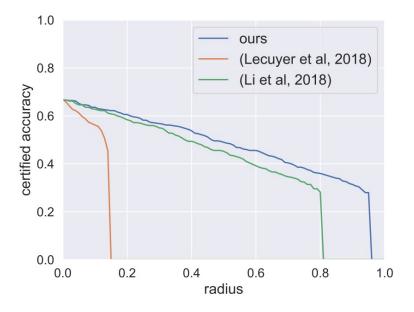


• Radius R vs. certified accuracy (by smoothing with σ)





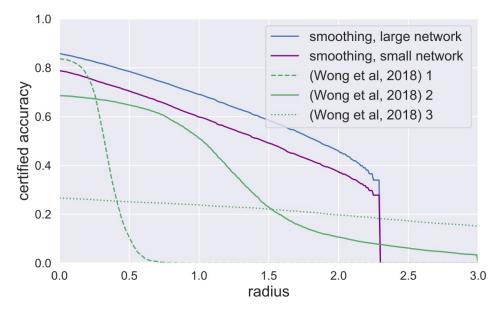
• Certified accuracy compared to prior work



 \leftarrow ImageNet, smoothed by $\sigma = 0.25$

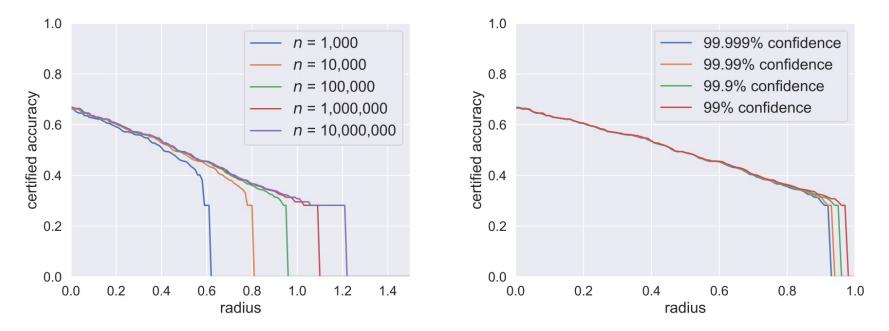


• Certified accuracy vs. other baselines





• Certified accuracy vs. { # samples or confidence }



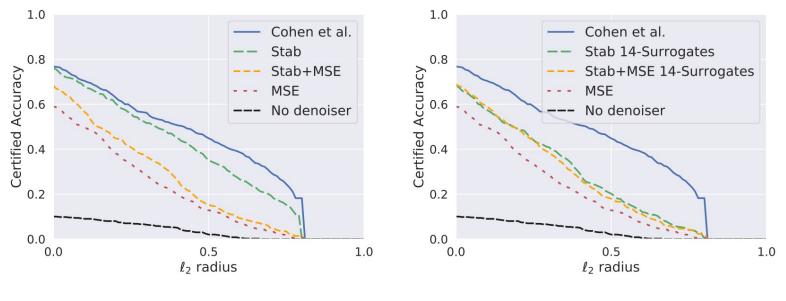
Evaluation: Denoised Smoothing

- Setup
 - ImageNet:
 - Pre-trained classifiers: ResNet-18/34/50 (white-box)
 - Baseline: ResNet-110 certified with $\sigma = 1.0$
 - Denoisers: DnCNN and MemNet trained with σ = 0.25, 0.5, 1.0
 - Objectives: MSE / Stab / Stab+MSE
 - White-box (as-is) | Black-box (14-surrogate models)
- Measure
 - (approximate) Certified test-set accuracy



Evaluation: Denoised Smoothing

• Radius R vs. certified accuracy (train denoisers with $\sigma = 0.25$)



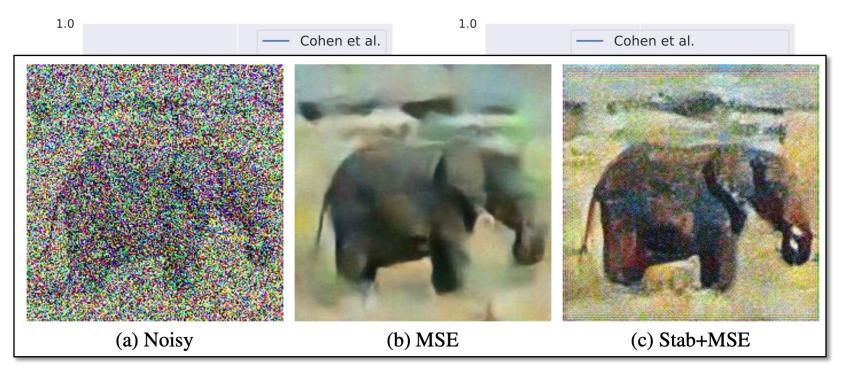
(a) White-box

(b) Black-box



Evaluation: Denoised Smoothing

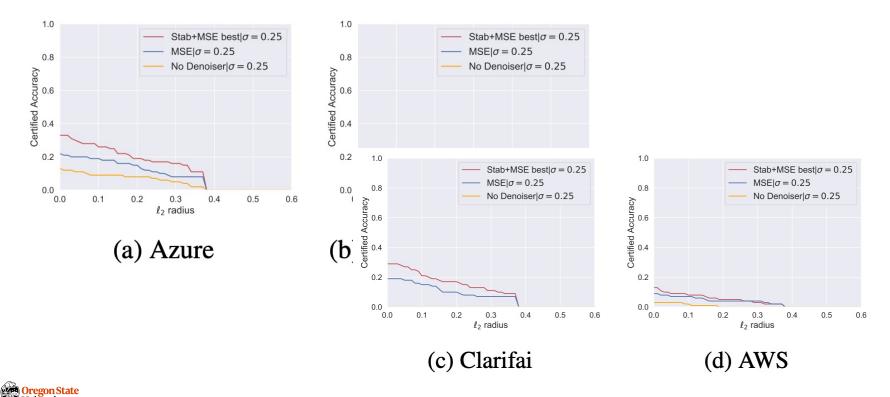
• Radius R vs. certified accuracy (train denoisers with $\sigma = 0.25$)





Evaluation: Denoised Smoothing in the Real-world

• Radius R vs. certified accuracy (train denoisers with $\sigma = 0.25$)



Conclusion

- Research Questions:
 - RQ 1: What is the "upper-bound" of the robustness?
 - Certified accuracy offered by randomized smoothing
 - RQ 2: How can you "certify" that yours is the upper-bound?
 - Predict and Certify functions
 - RQ 3: How can we make the certification "computationally feasible"?
 - Train a base classifier with smoothing
 - Train a denoiser with a base classifier, and attach it to the input



Topics Covered Today

- Certified (Provable) Defenses
 - Motivation
 - Robustness [?!]
 - Make ML models robust
 - Certified robustness
 - (Randomized) Smoothing
 - Guarantee
 - Practicality
 - Implementation
 - Evaluate the robustness
 - Upper-bound / Lower-bound
 - Real-world scenarios
 - Conclusions



Summary: Adversarial Examples

- ML Matters
- Evasion (Test-time Adversarial) Attack
 - Threat model
 - Attacks:
 - White-box:
 - FGSM / BIM / C&W / PGD attacks
 - Black-box:
 - Practicality
 - Transfer-based / Optimization-based attacks
 - Defenses:
 - Adversarial training
 - System-level defenses (e.g., FeatureSqueezing)
 - Certified (provable) defenses



Thank You!

Mon/Wed 12:00 – 1:50 pm

Sanghyun Hong

https://secure-ai.systems/courses/MLSec/W22



