## **CS 578: CYBER-SECURITY**

# PART I: BASIC CRYPTO FOR NETWORK/INTERNET SEC.

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# How can we do secure communication?

# **CRYPTO!**

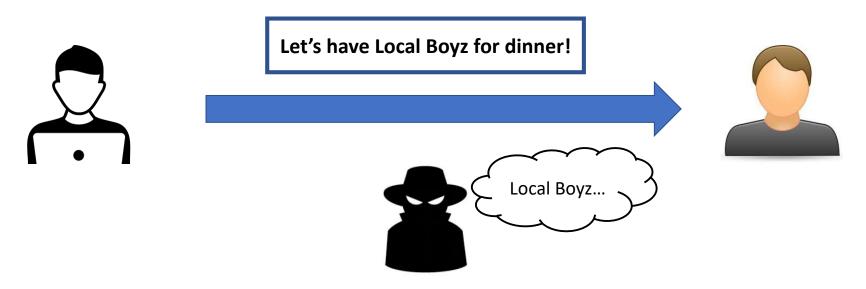
- Confidentiality
  - We want to communicate with others securely (and privately)





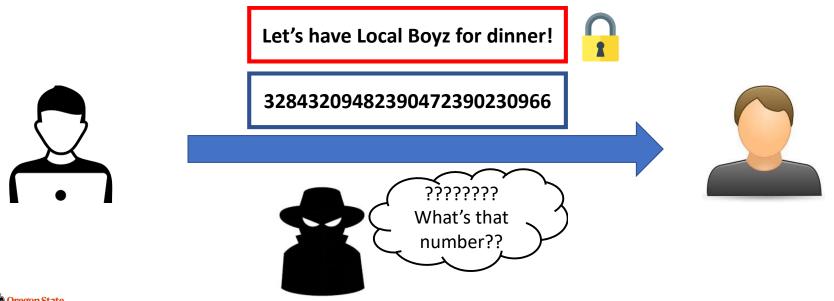
# **CRYPTO!**

- Confidentiality
  - We want to communicate with others securely (and privately)
  - Plaintext communication can be eavesdropped by an adversary



### CRYPTO!

- Confidentiality
  - We want to communicate with others securely (and privately)
  - Plaintext communication can be eavesdropped by an adversary
  - Cryptography enables secure (and private) communication



### **BASIC TERMINOLOGY**

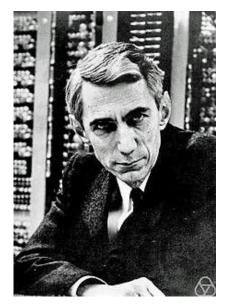
- Terms
  - Plaintext: readable text, before getting encrypted
  - Ciphertext: encrypted text, transformed plaintext using an encryption algorithm

 Encryption/decryption: the act of encrypting (or decrypting) Let's have Local Boyz for dinner! Local Boyz... 32843209482390472390230966 **5555555** What's that number??



### **PERFECT SECURITY**

- Shannon's intuition
  - An adversary should not distinguish a message M from a random text R

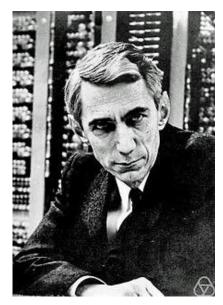


Claude Shannon (1916 ~ 2001) A Father of Information Theory and Modern Cryptography



### **PERFECT SECURITY**

- Shannon's intuition
  - An adversary should not distinguish a message M from a random text R
  - Formally:
    - Pr[M = m | C = c] = Pr[M = m]
    - where
      - m is a message (from a set M)
      - c is a ciphertext (from a set of all ciphertexts C)
    - Pr[C = c | M = m] = Pr[C = c]
  - It means:
    - Ciphertext provides no additional information
    - Observing c does not help with guessing M = m
    - c is independent of the message m



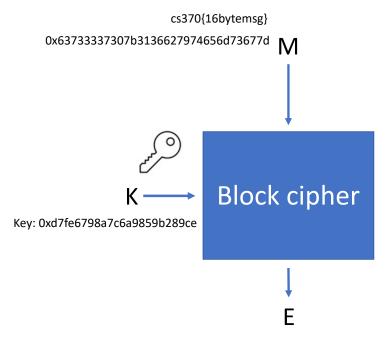
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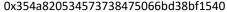


# How can we do perfectly secure in communication?

### **BLOCK CIPHER: ENCRYPTION**

- Block cipher
  - Cryptographic algorithm that work only with fixed-length set of bits
- Terminology
  - **Block:** a fixed size message *M*
  - **Key:** a secret we use for encryption
    - Shared between a sender and a receiver
  - Encryption: use K to convert M into E

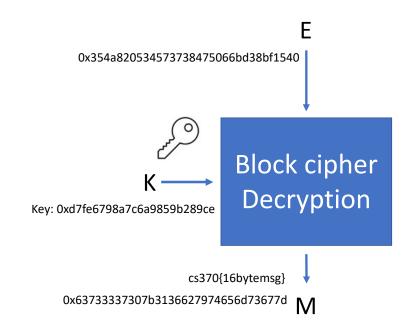






### **BLOCK CIPHER: DECRYPTION**

- Block cipher
  - Cryptographic algorithm that work only with fixed-length set of bits
- Terminology
  - **Block:** a fixed size message *M*
  - **Key:** a secret we use for encryption
    - Shared between a sender and a receiver
  - Encryption: use K to convert M into E
  - Decryption: use K to convert E into M



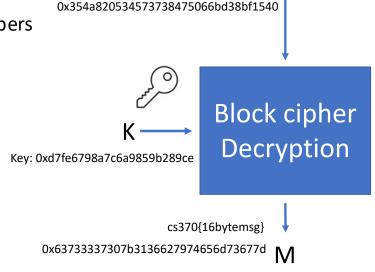


### **BLOCK CIPHER**

## Formally

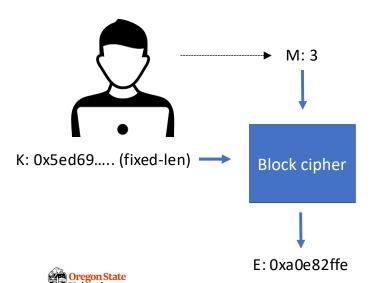
- You can see encryption and decryption as
- Generating a permutation of numbers:
  - $\{0,1\}^n \rightarrow \{0,1\}^n$
  - Mappings should be 1-to-1
- The key determines how to permute the numbers

М	Ciphertext
0	0xaf531b0e1
1	0x14a986e7a
2	0xad738009d
3	0x5ed6985c5
4	0xf3b8aa2e8
5	0xad04ec00e
	0x59fd94c21



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- Goal
  - We want to communicate with others securely (and privately)
  - Both parties use the same block cipher algorithm

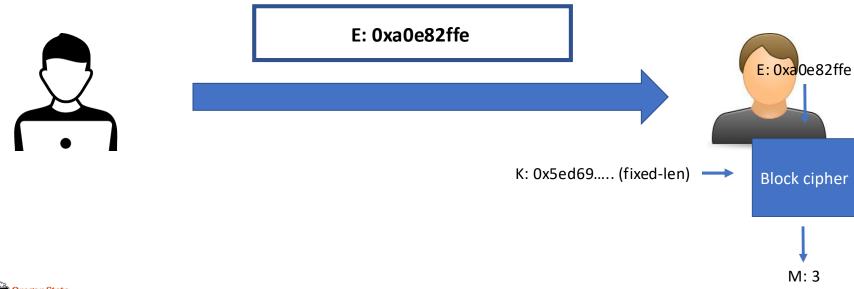




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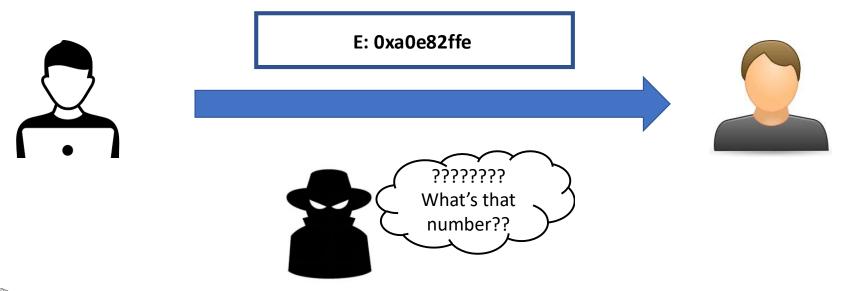


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- Goal
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  - Both parties use the same block cipher algorithm





# WHAT IS THE PROBLEM?

# **SYMMETRIC KEY CRYPTOGRAPHY**

#### Problems

- How can we securely share the key between two parties?
- How can we manage communications from/to multiple parties (100+)?





### SYMMETRIC KEY CRYPTOGRAPHY

#### Problems

- How can we securely share the key between two parties?
- How can we manage communications from/to multiple parties (100+)?

#### Solutions

- What if I have two keys?
  - Key A that only can encrypt a message (but can't decrypt)
  - Key B that can encrypt and decrypt a message
- How can I leverage the two keys?
  - Share Key A to others
  - Do not share; keep Key B private



- The key idea
  - Asymmetric key cryptography
  - Use two different keys for encryption and decryption
    - Public key: share to others, only can encrypt a message
    - Private key: do not share, can encrypt and decrypt
  - What is possible?

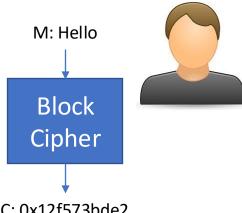






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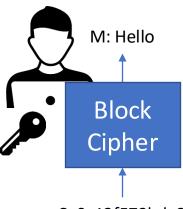






C: 0x12f573bde2

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- The key idea
  - Asymmetric key cryptography
  - Use two different keys for encryption and decryption
    - Public key: share to others, only can encrypt a message
    - Private key: do not share, can encrypt and decrypt
  - What is possible?
    - No one can decrypt a ciphertext unless they have the private key
    - We do not need to share the private key to anyone else
    - We share public key that can only encrypt the message



# PUBLIC KEY CRYPTOGRAPHY: ADVANTAGE

- Key exchange complexity
  - Each person shares their public key to everybody
  - But they do not share their private key
  - We need O(N) keys
- Benefit: it scales!
  - Suppose we have a crypto conference with 400 folks
  - Symmetric key crypto: we need 400 x 399 / 2 keys for secure comm.
  - Asymmetric key crypto: we only need 400 public-private key pairs



# WHAT ARE THE PUBLIC-KEY CRYPTO WE USE IN PRACTICE?

- RSA (Rivest, Shamir, Adleman)
  - A popular public key cryptography algorithm
  - It exploits the difficulty of prime factorization
    - To break RSA, an adversary solves the prime factorization of a large number
  - It is used for digital signature (we will revisit this later)



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## **RSA**

- Asymmetric key cryptography
  - Public key: e and N
  - Private key: d
- Key selection:
  - Choose two large prime number, p and q
    - Public key:
      - Set N = pq
      - Choose e as a coprime of  $\phi = (p-1)(q-1)$
    - Private key:
      - Find d that satisfies  $de == 1 \pmod{\phi}$



### **RSA**

- Key selection:
  - Choose two large prime number, p and q
    - Public key:
      - Set N = pq
      - Choose e (e.g., 65537) as a coprime of  $\phi = (p-1)(q-1)$
    - Private key:
      - Find d that satisfies  $de == 1 \pmod{\phi}$
- Security
  - Concern: can an adversary guess the private key from the public key?
  - To do such an attack, the attacker needs to find \u03c4
  - But we choose p and q as a large prime number; thus, it is difficult



# **RSA** ENCRYPTION

• Suppose we have

- Public key: e, N

- Message: M

- Ciphertext: Me mod N



### **RSA** DECRYPTION

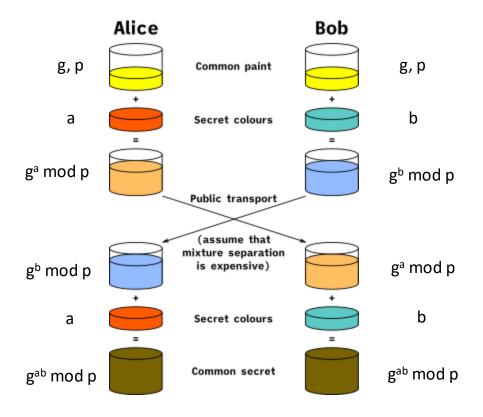
- We have
  - Public key: e, N
  - Message: M
  - Ciphertext: Me mod N
- Suppose we also have
  - Public key: e N
  - Private key: d (that satisfies ed = 1)
  - Ciphertext: C = M<sup>e</sup>
  - Plaintext: C<sup>d</sup> mod N
    - =  $(M^e)^d \mod N$
    - =  $M^{ed} \mod N$
    - = M mod N (N is a really large prime, so mostly it's N)



- Diffie-Hellman
  - A method of securely exchanging cryptographic keys over a public channel
  - Two parties can establish a shared secret (private) key over an insecure channel
- Security:
  - Based on the difficulty of mathematical problem of discrete logarithm



# **DIFFIE-HELLMAN KEY EXCHANGE IN GRAPHICS**





- Diffie-Hellman
  - A method of securely exchanging cryptographic keys over a public channel
  - Two parties can establish a shared secret (private) key over an insecure channel
- Security:
  - Based on the difficulty of mathematical problem of discrete logarithm
  - Example:
    - Given g, a, b, A, B, where
    - g<sup>a</sup> mod p = A
    - gb mod p = B
    - Can you compute g<sup>ab</sup> mod p?



- User A & User B agrees on g and p, where g and p are primes
- User A secretly chooses a, send A = g<sup>a</sup> mod p
- User B secretly chooses b, send B = g<sup>b</sup> mod p
- User A receives B, compute  $B^a = (g^b)^a \mod p = g^{ab} \mod p$
- User B receives A, compute  $A^b = (g^a)^b \mod p = g^{ab} \mod p$
- gab mod p is our secret

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• g<sup>ab</sup> mod p is our secret

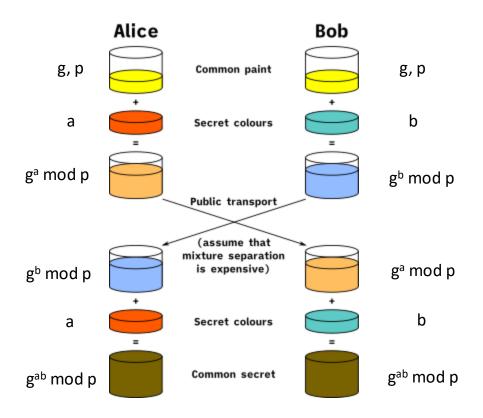
### • Suppose:

- Attacker knows g, p, A = g<sup>a</sup> mod p and B = g<sup>b</sup> mod p
- $-A+B = (g^a + g^b) \mod p$
- $-AB = g^{(a+b)} \mod p$

### • Security:

- Hard to compute gab from those values
- Discrete logarithm; can you guess a from A = g<sup>a</sup> mod p

## **DIFFIE-HELLMAN KEY EXCHANGE IN GRAPHICS**





### **DIFFIE-HELLMAN KEY EXCHANGE EXAMPLE**

- g = 5, p = 23
- A chooses a = 4
  - $-A = 5^4 \mod 23 = 625 \mod 23 = 4$
- B chooses b = 3
  - $-B = 5<sup>3</sup> \mod 23 = 125 \mod 23 = 10$
- $B^4 = 10^4 \mod 23 = 10000 \mod 23 = 18$
- $A^3 = 4^3 \mod 23 = 64 \mod 23 = 18$
- $5^{(4*3)} = 5^{12} \mod 23 = 18$

## **DIFFIE-HELLMAN KEY EXCHANGE: IMPLICATIONS**

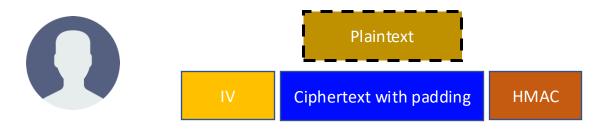
- Users are agreeing on two prime numbers
  - g, p
- User A chooses any integer a, nobody knows it
- User B chooses any integer b, nobody knows it
- By sharing g<sup>a</sup> mod P and g<sup>b</sup> mod p
  - Both shares g<sup>ab</sup> mod P without leaking a nor b

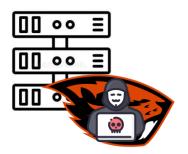
Two entities can interactively share a secret without directly leaking the secrets to others

## **DIGITAL CERTIFICATE AND ITS ECOSYSTEM**

#### **DIGITAL CERTIFICATE: MOTIVATION**

- An example scenario:
  - Suppose the oregonstate.edu server has the public/private key
  - You want to connect to the website securely



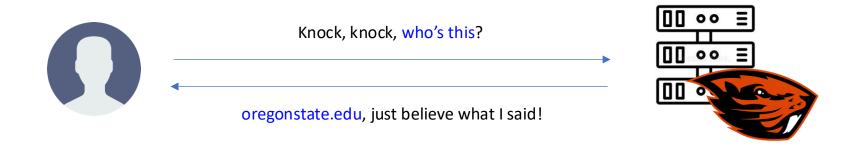


- Confidentiality: comes from the Block Cipher that we will use
- Integrity: comes from HMAC
- Where's authenticity?
  - How do you know the other end is oregonstate.edu?



### How can we check the authenticity?

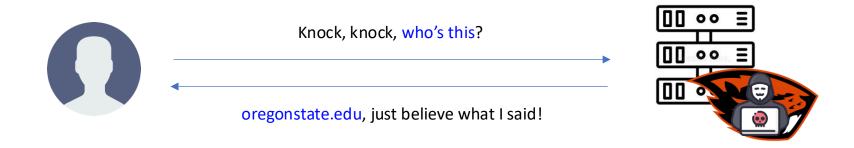
Can we check the other end is the one that we want to talk with?



We Need Some Ways to Check If They Are OSU (Authenticity)!

### How can we check the authenticity?

Can we check the other end is the one that we want to talk with?



We Need Some Ways to Check If They Are OSU (Authenticity)!



## How do we do that in the real-life?



### How can we do this for online communication?

#### Intuition

- Need an identification mechanism
- Need information that we can use to verify the sender

#### Solution

- Let's do this with RSA cryptography algorithm
- Let "oregonstate.edu" publicize the public key
- Let "oregonstate.edu" share their info. and signed by their private key



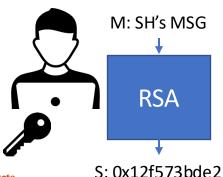
- Digital signature
  - A mathematical scheme for verifying the authenticity of digital messages
  - RSA can be used for "signing"
- Encryption and decryption for "signing"
  - Encryption is applying the private exponent to a plaintext: C = M<sup>d</sup> mod N
  - Decryption is applying the public exponent to a ciphertext: M = C<sup>e</sup> mod N





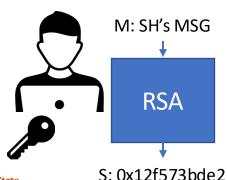


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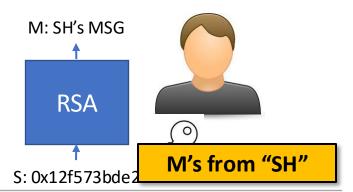
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#### How can we do this for online communication?

- Intuition
  - Need an identification mechanism
  - Need information that we can use to verify the sender
- Solution: Public Key Infrastructure (PKI)
  - Let's do this with RSA cryptography algorithm
  - Let "oregonstate.edu" publicize the public key
  - Let "oregonstate.edu" share their info. and signed by their private key
     (= we create a digital certificate)



## THE INFO: DIGITAL CERTIFICATE

- A file that contains
  - Entity info (CN)
  - Issuer info (CN)
  - Public key
  - Signature

#### Certificate Viewer: oregonstate.edu

General

Details

#### Issued To

Common Name (CN) oregonstate.edu

Organization (O) Oregon State University
Organizational Unit (OU) <Not Part Of Certificate>

#### Issued By

Common Name (CN)

Internet2

InCommon RSA Server CA

Organization (O)
Organizational Unit (OU)

InCommon

#### Validity Period

Issued On Expires On Sunday, June 5, 2022 at 5:00:00 PM Tuesday, June 6, 2023 at 4:59:59 PM

#### Fingerprints

SHA-256 Fingerprint 7B 57 A4 91 B0 06 29 2E 8E 54 04 FB BB F6 F8 4F

09 56 15 C0 20 59 37 9F E9 F1 A4 27 DC B6 F4 E1

SHA-1 Fingerprint FC EE 7C 4B AA 30 8F A6 03 E2 22 C5 31 FF 6C C6

92 FF C3 8E



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- Requester prepares a certificate request
  - Entity information
  - Public key
  - Signature (proving that I have the public key)

#### Certificate

CN: oregonstate.edu

Will use for:

\*.oregonstate.edu

Public Key: 0x112233445566778899aabbccddeeff.... (beaver's public key)

Signature: 0xaabbccddeeff00112233445566778899 (using beaver's private key)



- Requester prepares a certificate request
  - Entity information
  - Public key
  - Signature (proving that I have the public key)

Sign it with the private key

Get SHA256 sum of this part

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(using beaver's private key)



- Requester prepares a certificate request
  - Entity information
  - Public key
- Issuer verifies the requester information, and digitally sign the cert
  - Verify the entity information
  - Get a SHA-256 fingerprint of the certificate
  - Sign the fingerprint (with issuer's private key)

```
RSA_encrypt(private_key, SHA-256(certificate))
```



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- Anyone with the public key can verify the result
  - Get issuer's public key from their certificate



- The certificate requesting entity fills
  - Entity information
  - Public Key
- Entity:
  - For google, its \*.google.com
  - Can be your website address
- \*.secure-ai.systems
  - also has a certificate



CN = oregonstate.edu

Certificate

CN: oregonstate.edu

Will use for:

\*.oregonstate.edu

Public Key: 0x112233445566778899aabbccddeeff.... (beaver's public key)

Signature: Oxaabbccddeeff00112233445566778899 (with beaver's private key)



- The issuer receives the certificate request and verifies:
  - Entity
    - Their identification
    - Owning the target domain name
    - Owning the public key
  - The signature
    - Decrypt the signature with public key
    - It must be the same as SHA256 sum
    - It proves their holding the private key



Certificate

CN: oregonstate.edu

Will use for:

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Public Key: 0x112233445566778899aabbccddeeff.... (beaver's public key)

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- The issuer receives the certificate request and verifies:
  - Entity:
    - Their identification
    - Owning the target domain name
    - etc...
  - Then, fill issuer information
    - Issuer information
    - Issuer public key





CN = oregonstate.edu

Certificate

CN: oregonstate.edu

Will use for:

\*.oregonstate.edu

Public Key: 0x112233445566778899aabbccddeeff....

(beaver's public key)

Issuer: InCommon RSA

Public Key: 0x22334455667788990011aabbccddeeff



- The issuer receives the certificate request and verifies:
  - Entity:
    - Their identification
    - Owning the target domain name
    - etc...
  - Then, fill issuer information
    - Issuer information
    - Issuer public key
  - and then, sign the certificate
    - Get SHA-256 of the certificate
    - Attach it as a signature!





CN = oregonstate.edu

Certificate

CN: oregonstate.edu

Will use for:

\*.oregonstate.edu

Public Key: 0x112233445566778899aabbccddeeff....

(beaver's public key)

Issuer: InCommon RSA

Public Key: 0x22334455667788990011aabbccddeeff Signature: 0xffeeddccbbaa00112233445566778899

(InCommon RSA's private key)



#### THE CERTIFICATE ISSUED

- Now InCommon RSA verified
  - oregonstate.edu is owned by
  - Oregon State University
  - With a specific Public Key

▼ Subject Public Key Info

Subject Public Key Algorithm

Subject's Public Key

Field Value

Modulus (2048 bits):

C8 7D 2D A8 EB 12 59 6B 90 6D 4F 71 1E 4C FA C2 F7 A1 EC F6 E6 0E 39 52 FF 69 C0 36 CD A9 74 6E 60 72 C8 34 AF CC F7 6F 8E 66 D0 C5 0D E9 9C 66 F0 B2 D1 D8 75 A7 B9 82 E5 E8 C3 3F 13 35 1E 1E 71 F1 92 B4 40 07 EA 27 BE F9 9B AF E8 D2 E3 71

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09 56 15 C0 20 59 37 9F E9 F1 A4 27 DC B6 F4 E1 SHA-1 Fingerprint FC EE 7C 4B AA 30 8F A6 03 E2 22 C5 31 FF 6C C6

92 FF C3 8E

61

#### **RECAP: OSU CERTIFICATE**

- OSU owns "oregonstate.edu"
  - Verified by InCommon RSA
- Verification of the certificate
  - Use InCommon RSA's public key
  - Where is it? It is written in InCommon RSA's certificate
- But InCommon RSA, who will verify their identity?
  - InCommon RSA verifies "oregonstate.edu"
  - Who will verify InCommon RSA?



## LET'S SEE IT FROM THE BROWSER

- "oregonstate.edu"
  - Verified by InCommon RSA Server CA

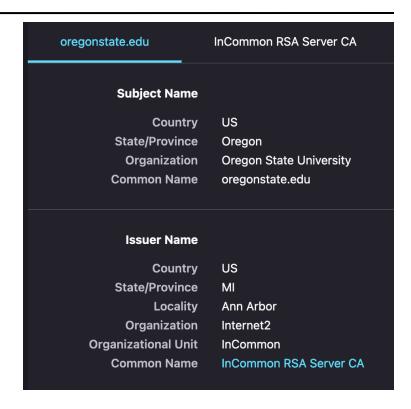
■ USERTrust RSA Certification Authority
 ■ InCommon RSA Server CA
 oregonstate.edu

- InCommon RSA Server CA
  - Verified by USERTrust RSA Certificate Authority
- USERTrust RSA CA
  - Verified by self



#### **TRUST CHAIN**

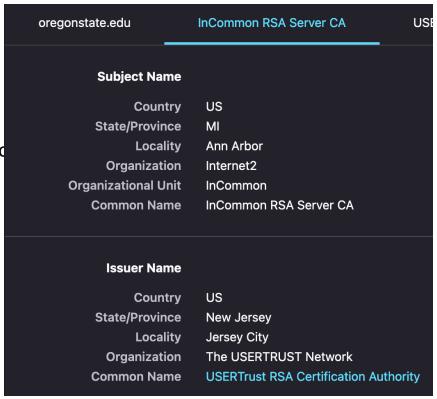
- "oregonstate.edu"
  - Verified by InCommon RSA Server CA
- InCommon RSA Server CA
  - Verified by USERTrust RSA Certificate Authority
- USERTrust RSA CA
  - Verified by self





### TRUST CHAIN - CONT'D

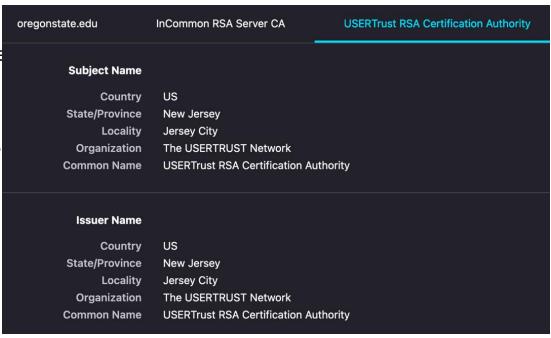
- "oregonstate.edu"
  - Verified by InCommon RSA Server CA
- InCommon RSA Server CA
  - Verified by USERTrust RSA Certificate Author
- USFRTrust RSA CA
  - Verified by self





### TRUST CHAIN - CONT'D

- "oregonstate.edu"
  - Verified by InCommon RSA Se
- InCommon RSA Server CA
  - Verified by USERTrust RSA Ce
- USFRTrust RSA CA
  - Verified by self





- An example:
  - Student
  - Oregon resident
  - U.S. Citizen
- When issuing the student ID
  - We verify your Oregon ID...



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- An example:
  - Student
  - Oregon resident
  - U.S. Citizen
- When issuing the student ID
  - Verify your Oregon ID...
- When issuing the Oregon Driver's License
  - Require either one of your birth certificate, previous Driver's License, or U.S. passport



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- An example:
  - Student
  - Oregon resident
  - U.S. Citizen
- When issuing the student ID
  - Verify your Oregon ID...
- When issuing the Oregon Driver's License
  - Require either one of your birth certificate, previous Driver's License, or U.S. passport
- When issuing the U.S. passport
  - Require your birth certificate or previously issued passport..



- An example:
  - Student
  - Oregon resident
  - U.S. Citizen

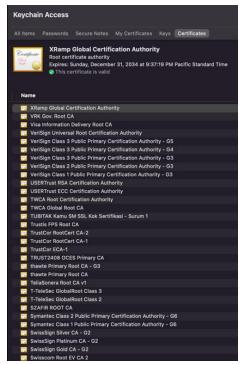
We need someone to verify the originality of the proving document...

- When issuing the student ID
  - Verify your Oregon ID...
- When issuing the Oregon Driver's License
  - Require either one of your birth certificate, previous Driver's License, or U.S. passport
- When issuing the U.S. passport
  - Require your birth certificate or previously issued passport..



## ROOT CERTIFICATE AUTHORITY (ROOT CA $\approx$ US in prev. example)

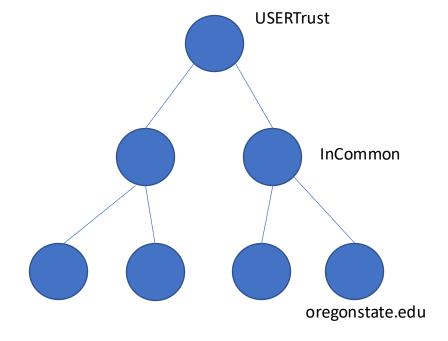
- Define small set of trustworthy certificate authorities
  - Private companies are authorized by some jurisdiction to run the CA company
    - Google Trust Service (GTS CA)
    - DigiCert
    - Verisign
    - etc..
- Trust their self-signed certificate
  - Stored in almost every computer machines





## PUBLIC KEY INFRASTRUCTURE (PKI)

- An Infrastructure that provides public key with certificate chain
- Trust anchor: Root CA
  - Set a small set of entities use self-signed cert
- Verify the certificate chain!
  - Must verify the entire chain



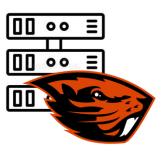


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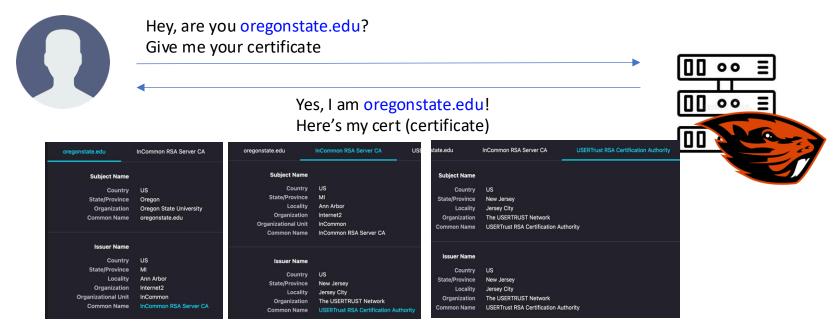
• Using the digital certificate!



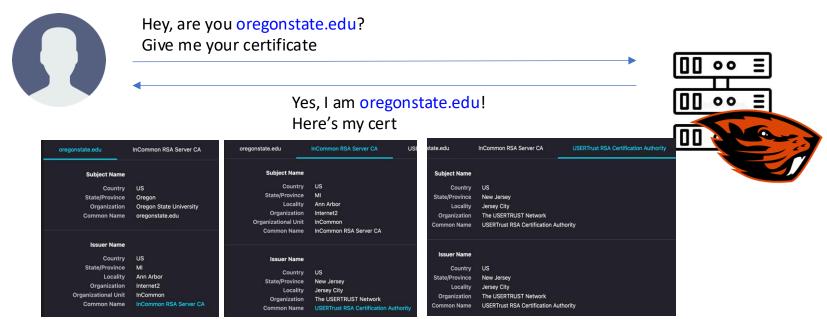
Hey, are you oregonstate.edu? Give me your certificate



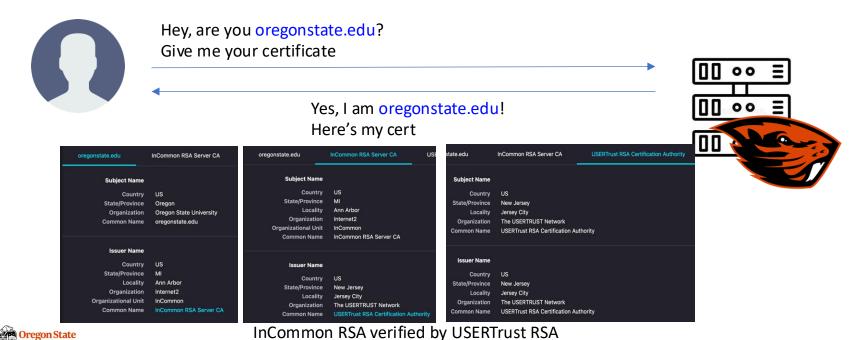
Using the digital certificate!



Using the digital certificate!

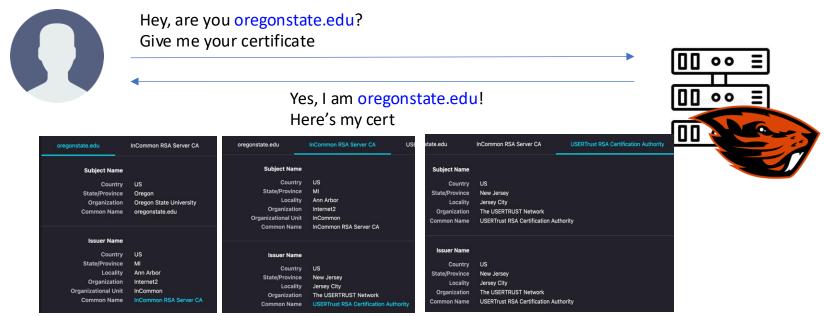


Using the digital certificate!



University

Using the digital certificate!



# **Thank You!**

#### Sanghyun Hong

https://secure-ai.systems/courses/Sec-Grad/current



